

Physics 780: Advanced Quantum Mechanics

Course Information:

Time: Wednesday 6.00pm –8.50 pm

Place: SMT 240

Instructor: Neepa T. Maitra

Phone: 973-353-1573

Email: neepa.maitra@rutgers.edu (*best way to reach me*)

Office hour: Weds 4.00pm—5.30pm, or by appointment, Rm 357 Smith Hall

Pre-requisites:

Sufficient proficiency with non-relativistic quantum mechanics is required.

Recommended Reading:

Gabriele F. Giuliani and Giovanni Vignale, “Quantum Theory of the Electron Liquid”, (Cambridge University Press, 2005)

E. K. U. Gross, E. Runge, and O. Heinonen, “Many-Particle Theory”, Institute of Physics Publishing (1991) (*an electronic version will be made available to students in the class*)

John P. Perdew and Stefan Kurth: “Density Functionals for Non-Relativistic Coulomb Systems”, in “A Primer in Density Functional Theory” Ed. C. Fiolhas, F. Nogueira, and M. Marques (Springer Lectures Notes in Physics, v.620, 2003). (*an electronic version will be made available to students in the class*)

E. K. U. Gross and N. T. Maitra: “Introduction to TDDFT”, in *Fundamentals of Time-Dependent Density Functional Theory*, eds. M. A. L. Marques, N.T. Maitra, F. Nogueira, E. K. U. Gross, and A. Rubio (Springer-Verlag, Berlin-Heidelberg, 2012). (*an electronic version will be made available to students in the class*)

In addition to these, journal and review articles will be recommended as we go along.

Grading:

Homework: 70%

There will be about 5 long problem sets, due about every two weeks, including in-class demonstrations of problem-solving.

Seminar Presentation: 30%

During the last few weeks, you will prepare a half-hour seminar on a topic, chosen from a list. These topics will have arisen during class but not covered in depth; you will provide a focused lecture on one of them during your seminar. A preliminary list of topics will be available by the 4th week of class.

Course Syllabus (Tentative):

1. Identical Particles and Many-Body Interactions in Quantum Mechanics
(Introduction to interactions in many-body QM, N-electron wavefunctions, operators, reduced variables, density operators, review of second quantization, Hubbard model)
2. Jellium
(translationally invariant Hamiltonians, high versus low-density regimes, weak interaction limit, exchange energy, rs-expansion, Wigner crystal, (charge-density and spin-density waves))
3. The Hartree-Fock Approximation
(Hartree-Fock equations, ground-state and excitation energies, exchange energy and correlation energy, symmetry-dilemma, application to jellium)
4. Linear Response Theory
(general response functions, spectral representations, analytic properties, sum-rules, density-response, Lindhard function, dielectric function, random phase approximation, plasmons)
5. Many-Body Perturbation Theory
(Time-ordered correlation function, Green's function and self-energy, screened interactions, Bethe-Salpeter equation, Hedin's equations, GW approximation)
6. Density Functional Theory
(Hohenberg-Kohn theorem, Kohn-Sham equations, exchange-correlation energy, exact properties of functionals, approximate functionals)
7. Time-Dependent Density Functional Theory
(Runge-Gross theorem, time-dependent Kohn-Sham, excitation energies, electron-energy-loss spectra, optical spectra of solids, adiabatic approximation, exact properties)
- (8. Phonons – if time allows)
(Born-Oppenheimer approximation, lattice vibrations, acoustic and optical phonons)